

Improved Spatial and Temporal Mobility Metrics for Mobile Ad Hoc Networks

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Abstract—This work shows that two well-known spatial and temporal mobility metrics for mobile ad hoc networks (MANETs) have drawbacks, possibly leading to invalid results. Based on the concept of spatial dependence in the absence of movement among mobile nodes, we propose mobility metrics able to promptly capture spatial and temporal dependence among mobile nodes. Through simulation, we compared the proposed metrics over a diversified set of synthetic mobility models. The results revealed that our spatial metrics can capture spatial dependence in scenarios having different levels of node pause time. Our temporal metric also demonstrated to be better suited for capturing different levels of temporal dependence, without being biased by node speed. Thus, the proposed mobility metrics can accurately capture spatial and temporal node behavior in MANETs.

Index Terms—ad hoc network; mobility metric; spatial dependence; temporal dependence;

I. INTRODUCTION

To support the growth and development of mobile ad hoc networks (MANETs), researchers from industry and academia have designed a variety of protocols, spanning the physical to the application layer. Analytic modeling and simulation are amongst the most used methods for evaluating MANET protocols. The former has limitations due to the lack of generalization, and the intrinsic high level of complexity [5]. The latter is by far the most used method for designing and evaluating MANET protocols.

A mobility model is one of the most important components in the simulation of MANETs. This component describes the movement pattern of mobile nodes (e.g., people, vehicles), impacting on protocol performance [2], [4], [11], [15], topology and network connectivity [3], [8], [16], data replication [10], and security [7]. Bai et al. [2] demonstrated that the performance of a protocol can vary dramatically depending on the adopted mobility model.

Mobility models can be classified into four categories: random, temporal-based, spatial-based (or group-based), and with geographic restriction [1] (Figure 1). Aiming at measuring quantitatively and qualitatively mobility models, one can use mobility metrics.

Bai et al. [2] proposed a framework to analyze the impact of mobility on performance of routing protocols for MANET. They proposed two metrics to quantify the spatial and temporal dependence of mobile nodes. Since then, several works have been based on these metrics for many purposes [13], [14],

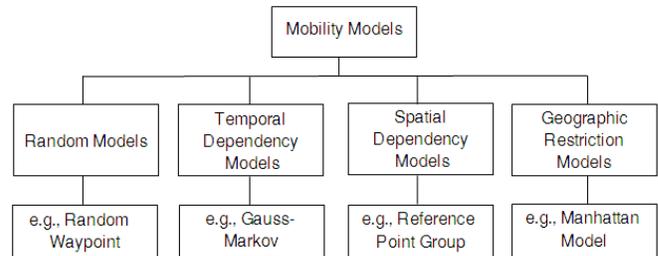


Fig. 1. Categories of mobility models in MANETs [1].

[17], [19], [20]. However, we show that those metrics have important drawbacks (Section III). After that, we introduce spatial and temporal metrics that overcome the described limitations, and also propose another spatial metric, based on the average distance among nodes (Section IV).

In order to evaluate the proposed metrics, we conducted an extensive simulation using four well know synthetic mobility models (Section V). Afterwards, we perform a comprehensive analysis of metrics behavior (Section VI).

II. TERMINOLOGY

The following terminology is needed to define the mobility metrics, and it will be used throughout this paper:

- T - Simulation time;
- N - Number of mobile nodes;
- X, Y - Length and width of the scenario;
- R - Radio communication range;
- $x(i, t)$ is the x-coordinate of node i at time t (idem for $y(j, t)$).
- $\theta(i, t)$ is the velocity angle of node i at time t .
- $v(i, t)$ is the velocity of node i in the time t and $v(i, t_0..t_k)$ means that the velocity of node i remains constant from t_0 to t_k .
- $Cos(i, j, t)$ is the cosine of angle between the velocities of nodes i, j :

$$Cos(i, j, t) = \frac{\vec{v}(i, t) \bullet \vec{v}(j, t)}{|\vec{v}(i, t)| \cdot |\vec{v}(j, t)|} \quad (1)$$

- $SR(i, j, t)$ is the speed ratio between nodes i, j at time t :

$$SR(i, j, t) = \frac{\min(\vec{v}(i, t), \vec{v}(j, t))}{\max(\vec{v}(i, t), \vec{v}(j, t))} \quad (2)$$

- $D(i, j, t)$ is the Euclidean distance between nodes i, j at time t :

$$D(i, j, t) = \sqrt{(x(j, t) - x(i, t))^2 + (y(j, t) - y(i, t))^2} \quad (3)$$

- $\rho(M_p, m)$: indicates the Pearson correlation between the parameter p of the mobility model M and the metric m .

III. RELATED WORK

Bai et al. [2] proposed, in their IMPORTANT framework, two mobility metrics that should be able to quantify spatial and temporal movement dependence among mobile nodes. Both metrics are based on the cosine similarity between the velocities of nodes (Equation 1).

The first one is the Degree of Spatial Dependence between nodes i, j at time t ($DSD(i, j, t)$), defined in Equation 4.

$$DSD(i, j, t) = \text{Cos}(i, j, t) \bullet SR(i, j, t) \quad (4)$$

Therefore, the average degree of spatial dependence (DSD) is given as the average between all nodes during the simulation. Group-based mobility models (e.g., RPGM [9]) should present high values for DSD .

The second mobility metric proposed by Bai et al. is the Degree of Temporal Dependence (DTD) (Equation 5), which is calculated similarly to DSD but it considers the difference of velocities between two time slots. Thus, the current velocity of a mobile node is dependent on its past moving pattern. This metric reflects the smoothness of node movement.

$$DTD(i, t, t') = \text{Cos}(\vec{v}(i, t), \vec{v}(i, t')) \bullet SR(\vec{v}_i(t), \vec{v}_i(t')) \quad (5)$$

Temporal mobility models (e.g., Gauss-Markov [12]) should present high values for DTD , while strongly random models should have null DTD (i.e., zero). For the former models, node velocity changes incrementally, unlike the abrupt changes occurring in random models (e.g., Random Waypoint).

Based on the work by Bai et al. [2], Zhang et al. [20] extended and developed the concept of a very similar spatial mobility metric, called Spatial Dependence (SD). The authors used this metric in the design of a distributed group mobility adaptive clustering algorithm (i.e., DMGA) [20]. However, both DSD and SD present the same limitation, which is described in next section.

A. Limitations on Previous Metrics

The main limitation on the DSD metric (Equation 4) is that it does not consider spatial dependence (correlation) in the absence of node movement. While two nodes i, j are pausing, their correlation is always zero (i.e., $Cor(i, j, t) = 0$), what is not necessarily true because nodes i and j might have paused (i.e., switched to velocity zero) just because there is some dependence between them.

To demonstrate that the assumption may be wrong, consider two mobile nodes, B and C, which are moving in accordance to the movement pattern of their leader, node A (Figure 2). At time t_0 , nodes B and C are inside node's A

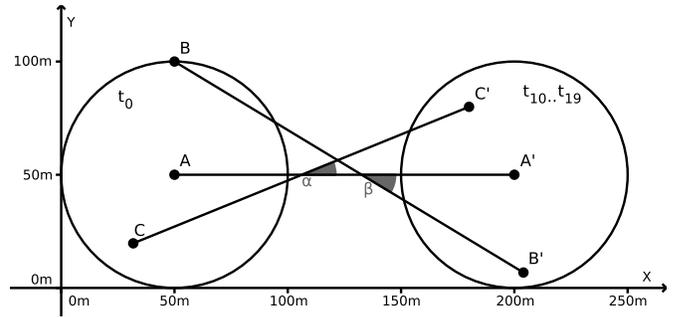


Fig. 2. Example of a group mobility scenario.

TABLE I
PAUSE CORRELATION PROBLEM IN A GROUP MOBILITY SCENARIO.

Nodes	Movement (t:0..9)	Pause (t:10..19)
	$v(i,t)$	
A	15 m/s	0 m/s
B	18 m/s	0 m/s
C	16 m/s	0 m/s
$DSD(i,j,t)$		
A,B	0.71	0
A,C	0.87	0
B,C	0.53	0

transmission range and they all start moving to points A', B', and C' where $v(A, t_0..t_9) = 15m/s$, $\theta(A, t_0..t_9) = 0$, $v(B, t_0..t_9) = 18m/s$, $\theta(B, t_0..t_9) = \beta$, $v(C, t_0..t_9) = 16m/s$ and $\theta(C, t_0..t_9) = \alpha$. By that time, they stop from t_{10} to t_{19} . For this group mobility scenario, the DSD metric just captures the correlation during the movement period (i.e., from t_0 to t_9), while the correlation is considered null during pause times (Table I). There is a clear spatial dependence among nodes during pause times, but it is not captured by the DSD metric. From t_0 to t_9 the total degree of spatial dependence is .7034. By time $t = 19$, DSD has decayed to .3517. In case the nodes continue paused for an additional 10 s, the DSD decreases to .2345. Thus, the higher the node pause time, the lower the metric value. Therefore, it is paramount considering the correlation during pause periods.

IV. CONTRIBUTIONS

We propose the *Improved Degree of Spatial Dependence* (IDSD), a spatial mobility metric which is able to capture both movement and pause correlation among mobile nodes.

The second contribution is the proposal of the *Improved Degree of Temporal Dependence* (IDTD), a temporal mobility metric based on DTD [2]. Besides the pause correlation problem, DTD was not able to distinguish temporal from atemporal mobility models [2]. We verified that this is due to improperly computing that metric: instead of computing $DTD(i, j, t)$ for each time slot t , it should only be computed when the velocity $v(i, t)$ changes in magnitude or direction. With this simple modification, IDTD can, in addition to other benefits, distinguish temporal and atemporal mobility models.

IDTD is also substantially less impacted by node speed. In addition to that, it has higher correlation to parameter

α , a memory level parameter commonly defined in temporal models such as Gauss-Markov [12] and Semi-Markov Smooth [21].

Our third contribution is a novel spatial mobility metric, named Degree of Node Proximity (DNP), which is capable of distinguishing group-based mobility models from others. Besides that, simulation results show that *DNP* is less impacted by node pause time than *DSD*.

A. Pause State Movement Dependence

It is reasonable to consider that spatial dependence between two nodes i, j at a pause time step t , $DSD(i, j, t)$, will be equal to the average of the last K values. The higher the average pause time, greater is the value of K . Thus, the Improved Degree of Spatial Dependence metric equation is given by:

$$IDSD(i, j, t) = \begin{cases} PC(i, j, t) & \text{if } \vec{v}(i, t) = \vec{v}(j, t) = 0, \\ DSD(i, j, t) & \text{otherwise.} \end{cases} \quad (6)$$

where $PC(i, j, t)$ is the pause correlation between nodes i, j at time t . It is computed as follows:

$$PC(i, j, t) = \frac{1}{K} \sum_{k=t-K}^{t-1} DSD(i, j, k) \quad (7)$$

where K is a function of the average pause time, a typical mobility model input parameter¹.

B. Improved Degree of Temporal Dependence

As explained previously, the metric *DTD* (Equation 5) should be computed only when the node velocity changes, otherwise, it will not be able to promptly catch the temporal node behavior of a mobility model. Thus, we have that $IDTD(i, t) = 0$ if $v(i, t) = v(i, t-1)$ and $\theta(i, t) = \theta(i, t-1)$, and $IDTD(i, t) = DTD(i, t)$ otherwise. Therefore, the Improved Degree of Temporal Dependence (*IDTD*) metric is defined as follows:

$$IDTD = \frac{1}{P} \sum_{i=1}^N \sum_{t=1}^T IDTD(i, t) \quad (8)$$

where P is the number of tuples (i, t) such that $IDTD(i, t) \neq 0$.

C. Degree of Node Proximity

We propose a spatial mobility metric based on the distance between pairs of nodes, called Degree of Node Proximity (*DNP*). Let AD be the average distance between all nodes during the simulation, and MAD be the maximum average distance expressed in units of transmission range, R . Formally speaking:

¹In fact, some mobility models have the maximum pause time (*MPT*) parameter instead of average pause time (*APT*). For those cases, pause time generally has an uniform probability distribution function, and then $APT = MPT/2$.

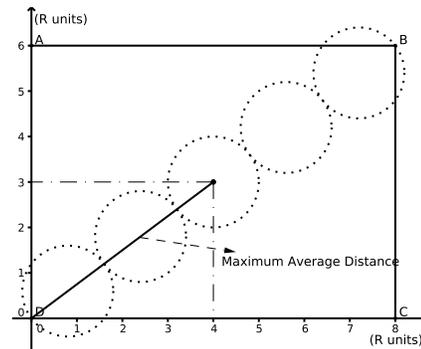


Fig. 3. Example of Maximum Average Distance (MAD).

$$AD = \frac{1}{N(N-1)/2} \sum_{i=1}^N \sum_{j=i+1}^N \frac{\sum_{t=1}^T D(i, j, t)/R}{T} \quad (9)$$

$$MAD = \frac{\sqrt{X^2 + Y^2}}{2R} \quad (10)$$

Suppose a scenario where its width is 600 m, its length is 800 m, and the node transmission range is 100 m. Then, the maximum average distance, MAD , is given by $5R$ (or 500 m). Figure 3 illustrates exactly this situation.

The proportion about AD and MAD gives a notion about the degree of mobility dependence. When the average distance among the nodes is constantly low, then this probably means that nodes follow some sort of group-mobility movement. For this reason, we define our spatial mobility metric *DNP* as expressed in Equation 11.

$$DNP = 1 - \frac{AD}{MAD} \quad (11)$$

DNP values normally range from 0 to 1. Spatial mobility models (e.g., RPGM [9]) should present high *DNP* values, while other models should present lower values. Next, we present an extensive simulation using these metrics and a heterogeneous set of mobility models.

V. SIMULATION

To verify the ability that our proposed mobility metrics have to capture spatial and temporal dependence among mobile nodes, we selected the following mobility models (the same displayed in Figure 1):

- Random Waypoint (RWP) [6]: is probably the simplest and most used mobility model in MANET simulation studies. It has just three parameters: minimum and maximum speeds, and maximum pause time.
- Reference Point Group Mobility (RPGM) [9]: is a group-based model where the movement of the leader of a group influences the movement of all its members. The distance between the leader and his members should not be greater than a threshold, called maximum distance from center (*MDC*). RPGM is more applicable for battle field or rescue operations scenarios.

TABLE II
MOBILITY MODELS SELECTED FOR SIMULATION.

Feature	RWP [6]	RPGM [9]	GM [12]	MAN [2]
Randomness	high	moderate	variable	moderate
Group-based		X		
Temporal			X	
Grid-based				X

- Gauss-Markov (GM) [12]: in this model the velocity of mobile node is assumed to be correlated over time and modeled as a Gauss-Markov stochastic process. *GM* is a temporally dependent mobility model whereas the degree of dependency is determined by the memory level parameter α ($0 < \alpha < 1$).
- Manhattan (MAN) [2]: is a grid-based model where nodes follow specific paths (e.g., streets) distributed in a rectangular grid. It is suitable for modeling the movement of vehicular wireless networks.

The results presented in this paper depend on some assumptions which are required for computing mobility metrics:

- Communication between nodes is always bidirectional during the simulation.
- R is constant and equal for all nodes.
- N is constant during the simulation.
- The scenario has a two-dimensional square geometry.

Table II summarizes the main characteristic of the selected mobility models. RPGM and MAN models are classified as having moderate randomness. The former, because the movements of regular nodes are limited to their leader's, and in the latter node movements are limited due to obstacles spread over the scenario (e.g., city blocks). Gauss-Markov (GM) presents variable randomness, since it depends on the value of the memory parameter α .

BonnMotion [18] was employed for mobility scenario generation producing the synthetic traces for the mobility models. For all scenarios, 100 nodes moved over an area of 1000m x 1000m for a period of 900 seconds. Transmission range was set to 100, 150, and 200 meters. For the RPGM model, the number of nodes per group (NG) was set to 10, 25, and 50, which represents scenarios with 2, 4, and 10 groups of mobile nodes. Maximum pause time and memory parameter were set to a large range of values (see Table III).

All graphs present results with a confidence level of 99%, based on 10 repetitions for each one of more than 1,400 generated mobility scenarios. In some situations, the interval length is smaller than the symbol used in the legend, making it barely visible.

VI. ANALYSIS

Firstly, we compare the performance of the temporal metrics DTD and $IDTD$. Then we show how the node pause time affects the spatial metrics DSD and $ISDS$. Lastly, we also show that our proposed metric, degree of node proximity (DPN), is able to differentiate the mobility models used in our simulation, and that it is not impacted by node pause time.

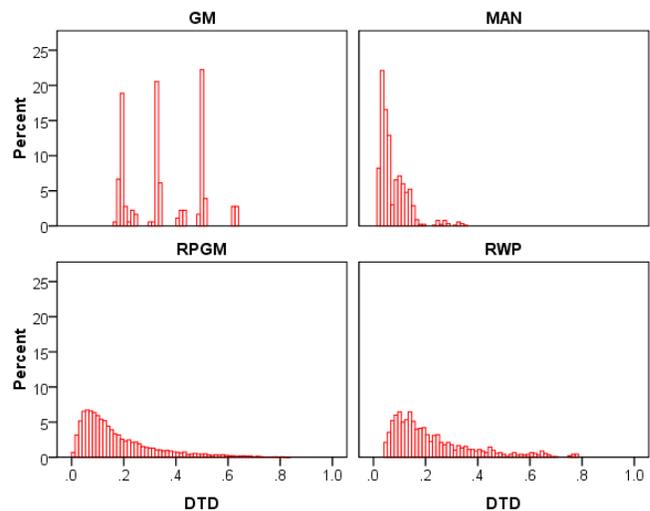


Fig. 4. Degree of Temporal Dependence (DTD) percentage histograms.

A. Temporal Metrics

Table IV shows the basic descriptive statistics for the mobility metrics. In general, random models showed moderate DTD values, what was not expected. For some scenarios, the DTD value for Random Waypoint and RPGM even surpassed GM's. The percentage histogram of DTD clearly reveals this shortcoming (see Figure 4). On the other hand, $IDTD$ properly identified the Gauss-Markov model as the unique temporal model among all under consideration, and the metric correctly considered that the other models should have values close to zero (Table IV).

The second problem with DTD metric is that it is very little impacted when changing the memory parameter α in the Gauss-Markov model (Figures 5, 6, and 7). The unique visible change happened when $\alpha = .99$. However, $IDTD$ demonstrated a higher correlation with α (.91 versus .35, Table V), and consequently is better in capturing different levels of temporal dependence than DTD .

The third problem is that DTD decreases with the increment of node speed. When maximum node speed (S) is 10 m/s, DTD is, on average, nearly 0.5. When S increases from 20 to 30, DTD decreases from 0.3 to 0.2 (Figures 5, 6, and 7). Nevertheless, this relationship is almost imperceptible with the $IDTD$ metric.

B. Spatial Metrics

As stated in Section III-A, the degree of spatial dependence DSD does not capture pause state spatial dependence (presented in Section IV-A).

Figure 8 shows the different effect that the variation of maximum node pause time MPT causes on DSD and $ISDS$ in the RPGM model with 10 groups of 10 nodes each. At point $MPT = 0$, both DSD and $ISDS$ have the same value, because nodes never stop moving. As the node pause time increases, DSD quickly decreases. However, $ISDS$ increases a little bit and keeps at about the same level

TABLE III
 CONFIGURATION OF MOBILITY MODELS' INPUT PARAMETERS FOR SIMULATION.

PARAMETER - unit	Gauss-Markov [12]	Random Waypoint [6]	RPGM [9]	Manhattan [2]
Simulation Time (T) - s	900			
Number of nodes (N)	100			
Transmission range (R) - m	100, 150, 200			
Scenario's length (X) - m	1000			
Scenario's width (Y) - m	1000			
Minimum speed (s) - m/s	1, 3, 5			
Maximum speed (S) - m/s	10, 20, 30			
Average speed (AS) - m/s	$f(S)^a$			6, 11, 16
Speed Standard Deviation (SSD)	$f(S,AS)^b$			$f(s,AS)^c$
Maximum pause time (MPT) - s	0, 100, 200, 300, 400, 500, 600, 700, 800, 900			
Number of nodes per group (NG)			10, 25, 50	
Memory Parameter (α)	.0, .2, .4, .6, .8, .99			
Number of rows (NR)				10
Number of columns (NC)				10
Max. deviation from leader (MDC) - R			1	
Speed change probability (SCP)				10%
Total number of experiments	2,700	540	8,100	2,700

^a It is a function of maximum speed (S).

^b It is a function between average (AS) and maximum speed (S).

^c It is a function between average (AS) and minimum speed (s) for MAN model.

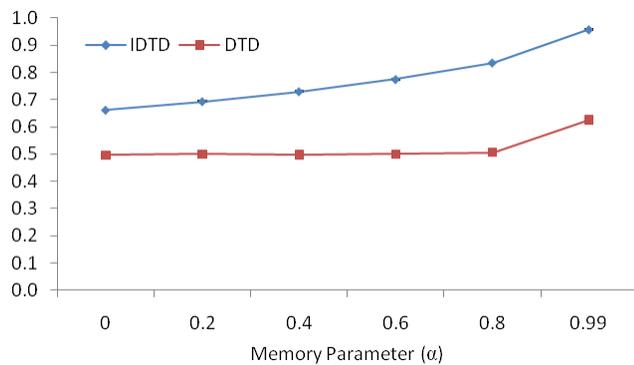


Fig. 5. Effect of memory parameter on the temporal mobility metrics ($S = 10m/s$, $R = 150m$).

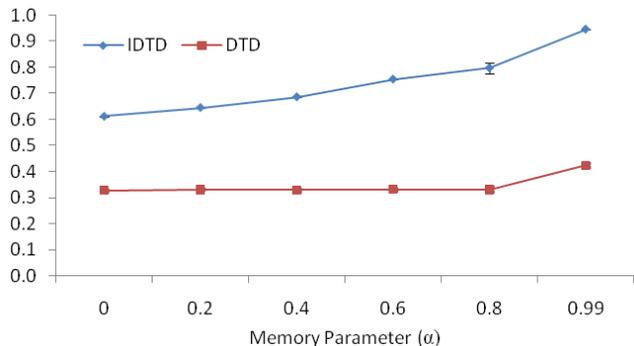


Fig. 6. Effect of memory parameter on the temporal mobility metrics ($S = 20m/s$, $R = 150m$).

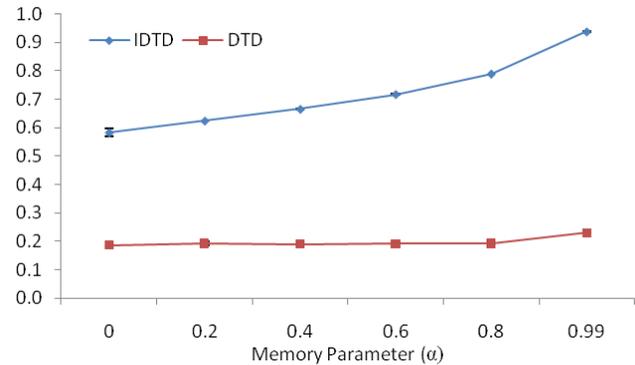


Fig. 7. Effect of memory parameter on the temporal mobility metrics ($S = 30m/s$, $R = 150m$).

until $MPT = 500s$, when then it starts decreasing. Similar behavior also happens in Figures 9 and 10. Although $IDSD$ also decreases, this occurred in a much more slower fashion than occurred with DSD . This is due to the smaller correlation between MPT and $IDSD$ ($\rho(RPGM_{MPT}, DSD) = -.58$ and $\rho(RPGM_{MPT}, IDSD) = -.32$, Table V).

Therefore, $IDSD$ presents more accurate values for spatial dependence among nodes than DSD . For most real scenarios, where MPT is low or moderate, $IDSD$ keeps nearly the same value as for $MPT = 0$. Even in unusual scenarios, where nodes stay longer paused than moving, $IDSD$ still presents higher spatial dependence values.

Concerning our second spatial mobility metric, Degree of Node Proximity (DNP), its histogram clearly distinguished the spatial dependency model (RPGM) from others, and showed similar patterns for RWP and MAN models (Figure 11). GM presented the lowest DNP standard deviation.

Figure 12 shows the effect that MPT causes on DNP for all the mobility models that have that input parameter.

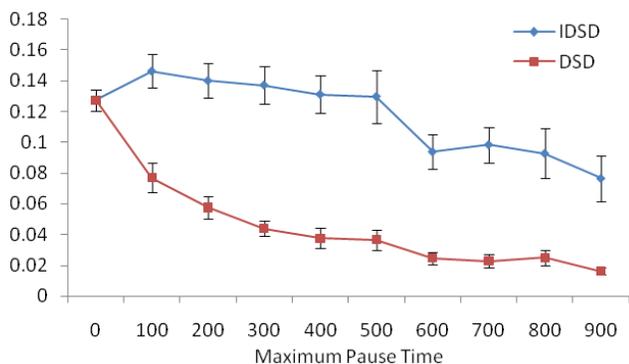


Fig. 8. Effect of pause time on the spatial mobility metrics in RPGM with 10 groups ($s = 3m/s, S = 20m/s, R = 150m$).

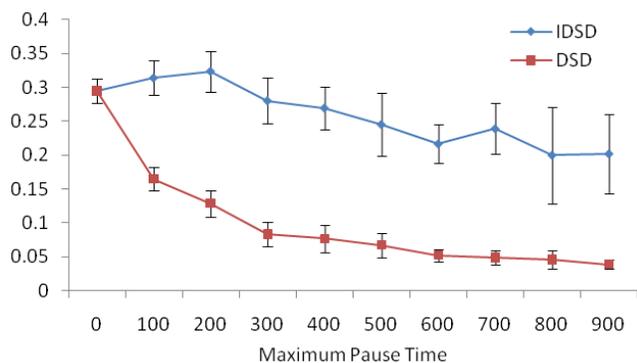


Fig. 9. Effect of pause time on the spatial mobility metrics in RPGM with 4 groups ($s = 3m/s, S = 20m/s, R = 150m$).

In the RPGM model, MPT caused a constant small drop in DNP . In the RWP model, DNP has a considerable drop for $MPT = 100s$, but then it remains approximately constant. On the other hand, the DNP in the MAN model was little affected by MPT .

Comparing the relationship between $IDSD$ and MPT , and between DNP and MPT , the difference is that in the last one, there is a constant small decay of DNP , instead of in

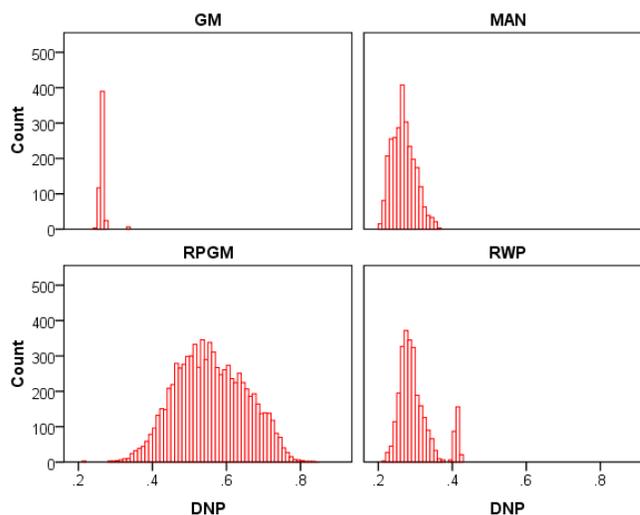


Fig. 11. Histogram-DNP.

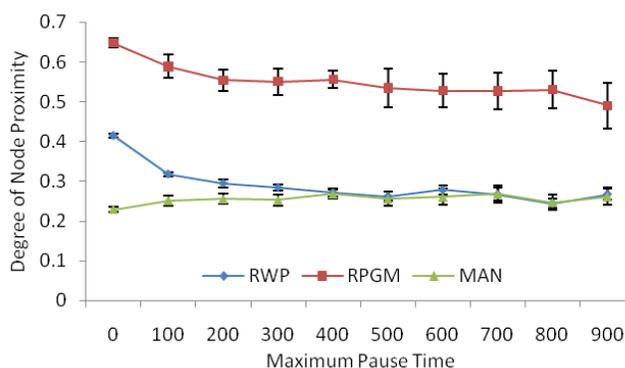


Fig. 12. Effect of pause time on the degree of node proximity metric.

the $IDSD$, when it starts to decay for higher MPT values. Anyway, both $IDSD$ and DNP are better than DSD , as they are extensively less affected by MPT .

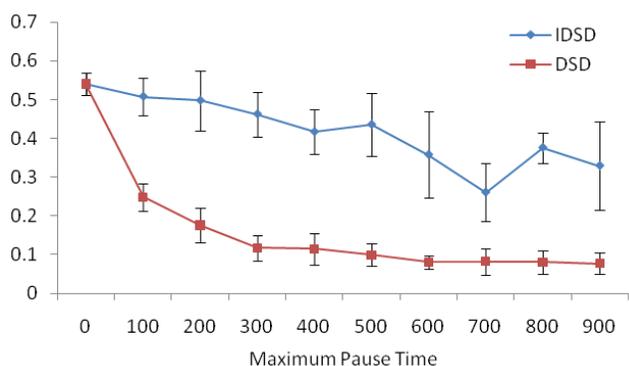


Fig. 10. Effect of pause time on the spatial mobility metrics in RPGM with 2 groups ($s = 3m/s, S = 20m/s, R = 150m$).

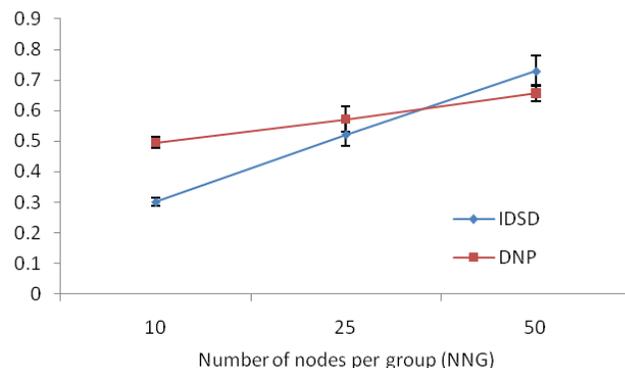


Fig. 13. Effect of number of nodes per group on metric $IDSD$ and DNP (RPGM).

TABLE IV
 DESCRIPTIVE STATISTICS FOR THE MOBILITY METRICS.

Metric	Model	Mean	STD	Min	Max
Degree of Spatial Dependence (<i>DSD</i>)	RWP	.007	.005	-.008	.029
	RPGM	.117	.126	.005	.805
	GM	.001	.005	-.012	.017
	MAN	.013	.012	-.004	.058
Degree of Temporal Dependence (<i>DTD</i>)	RWP	.226	.157	.042	.783
	RPGM	.175	.143	.003	.833
	GM	.355	.137	.17	.632
	MAN	.076	.056	.02	.353
Improved Degree of Spatial Dependence	RWP	.010	.006	-.008	.032
	RPGM	.279	.176	.024	.881
	GM	.001	.005	-.012	.017
	MAN	.017	.011	-.004	.059
Improved Degree of Temporal Dependence	RWP	.000	.000	.000	.001
	RPGM	.000	.000	.000	.003
	GM	.744	.112	.53	.958
	MAN	.012	.025	.001	.105
Degree of Node Proximity (<i>DNP</i>)	RWP	.299	.044	.245	.415
	RPGM	.558	.080	.374	.744
	GM	.271	.023	.261	.337
	MAN	.268	.023	.223	.321

 TABLE V
 CORRELATION MATRIX BETWEEN INPUT PARAMETERS AND MOBILITY METRICS.

Metric	Model	R	s	S	AS	MPT	NG	α
<i>DSD</i>	RWP	.18	.00	-.64		.25		
	RPGM	-.33	-.09	-.16		-.58	.38	
	GM	-.07		.08	.08			-.17
	MAN	.16	.02		-.66	-.06		
<i>DTD</i>	RWP	-.66	-.12	-.14		-.28		
	RPGM	-.11	-.37	-.39		-.66	.00	
	GM	.72		-.28	-.28			.35
	MAN	-.54	-.04		-.25	-.32		
<i>IDSD</i>	RWP	-.06	.04	-.64		.31		
	RPGM	-.59	.00	-.05		-.32	.67	
	GM	-.07		.08	.08			-.17
	MAN	.05	.02		-.68	.00		
<i>IDTD</i>	RWP	.00	.10	.05		-.51		
	RPGM	.07	.10	.04		-.51	.00	
	GM	.00		-.23	-.23			.91
	MAN	.00	.03		.06	-.58		
<i>DNP</i>	RWP	.00	-.06	-.12		-.82		
	RPGM	.24	.01	-.03		-.49	.77	
	GM	.00		-.22	-.22			.31
	MAN	.00	-.00		.36	.69		

VII. CONCLUSION AND FUTURE WORK

In this paper we introduced the concept of pause state movement dependence, which considers the possible existence of spatial dependence among nodes in a mobile ad hoc network (Section IV-A). From this concept, we proposed the Improved Degree of Spatial Dependence (*IDSD*) mobility metric. *IDSD* revealed to be better than *DSD* [2] at capturing the spatial dependence in scenarios having different patterns of node pause times (Section VI-B).

We also proposed another spatial mobility metric, Degree of Node Proximity *DNP*, which also presented better results than *DSD*. Besides this, we also proposed a new temporal mobility metric, called Improved Degree of Temporal Dependence (*IDTD*) that demonstrated to be better than *DTD* [2] in three aspects: capturing different levels of temporal de-

pendence, properly identified the Gauss-Markov model as the unique temporal model among all under consideration in this work, correctly setting other models to produce values near zero, and it is not influenced by node speed.

For future work we plan to investigate the use of the proposed mobility metrics in the design of mobility-aware adaptive routing protocols for mobile ad hoc networks.

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